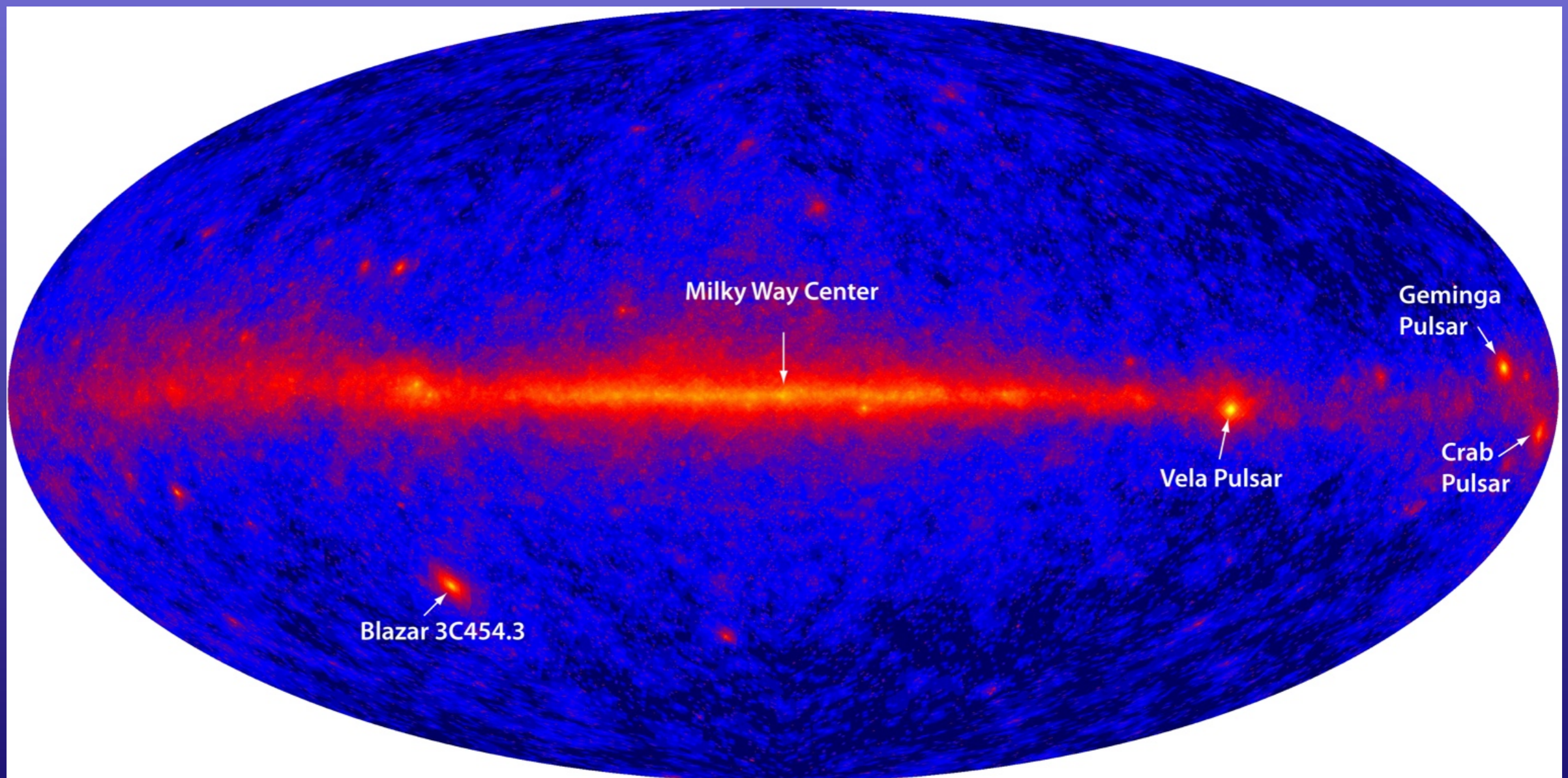


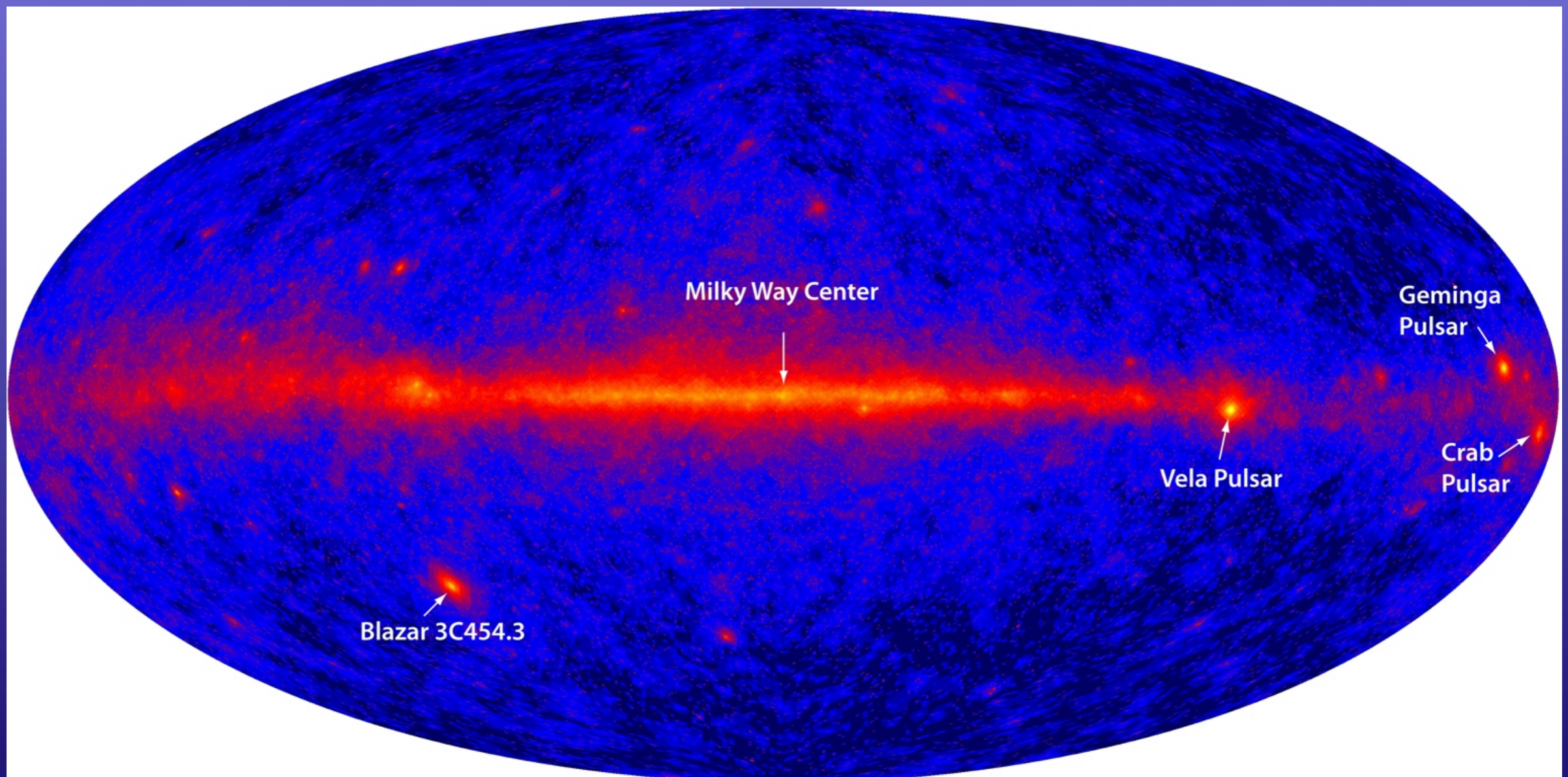
# QUANTIFYING, SUMMARIZING, AND REPRESENTING 'TOTAL' UNCERTAINTIES IN IMAGE (AND SPECTRAL) 'DECONVOLUTION'

A. Connors for 'CHASC' or CBASC








# PART II: DOUBT

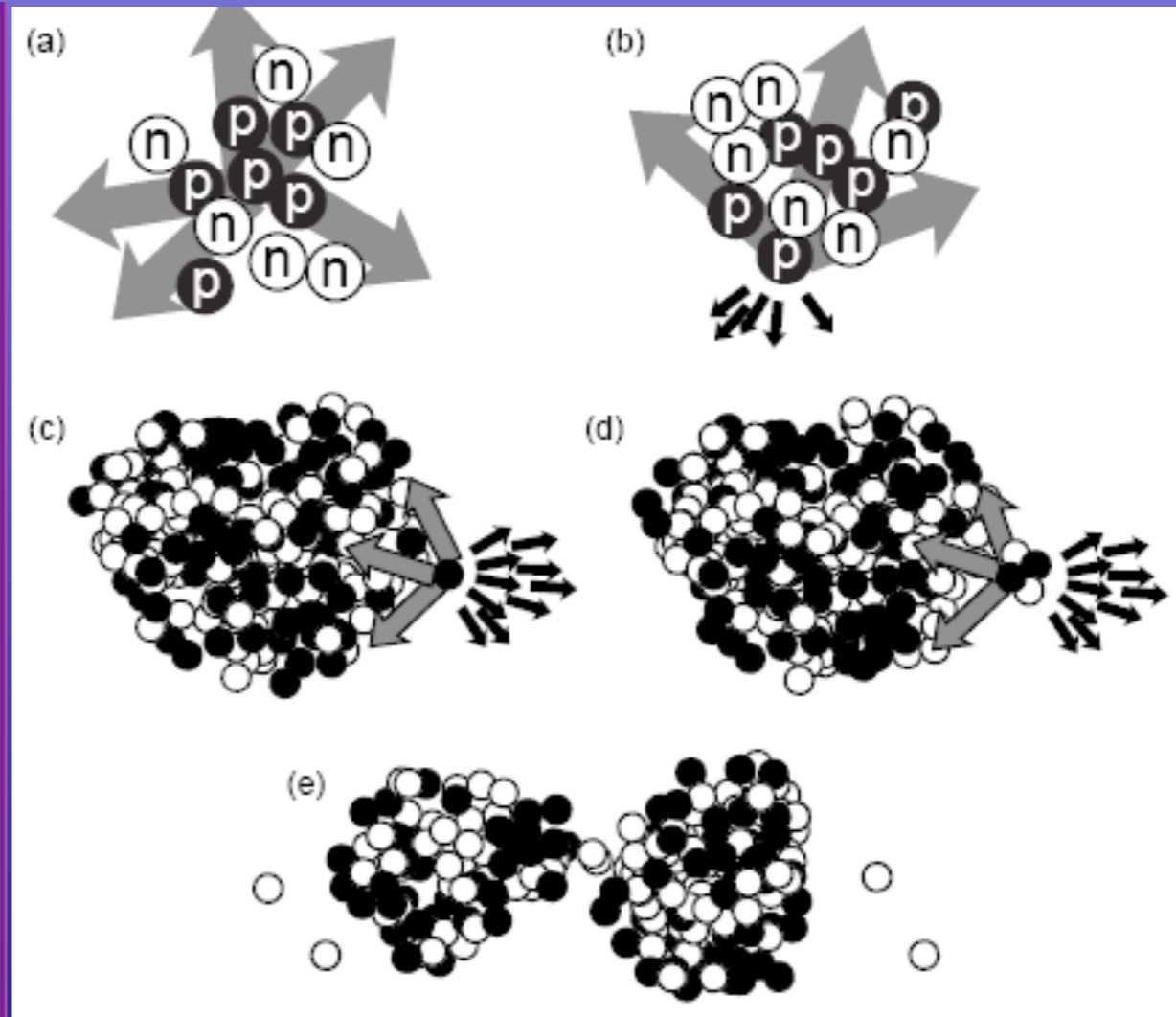
## A. Connors for 'CHASC' or CBASC

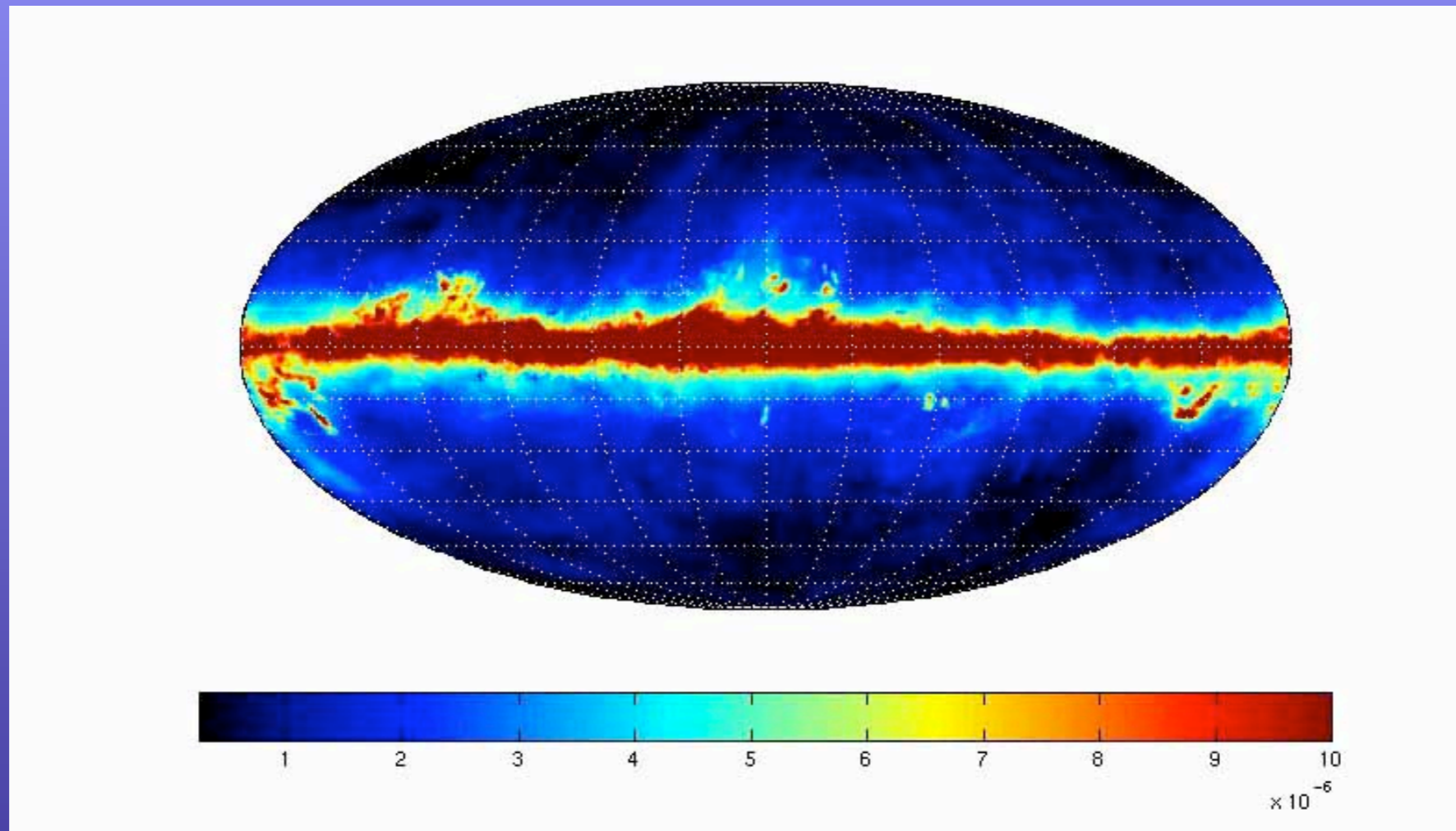


# INSIDE the source: Intrinsically Multinomial/Poisson?

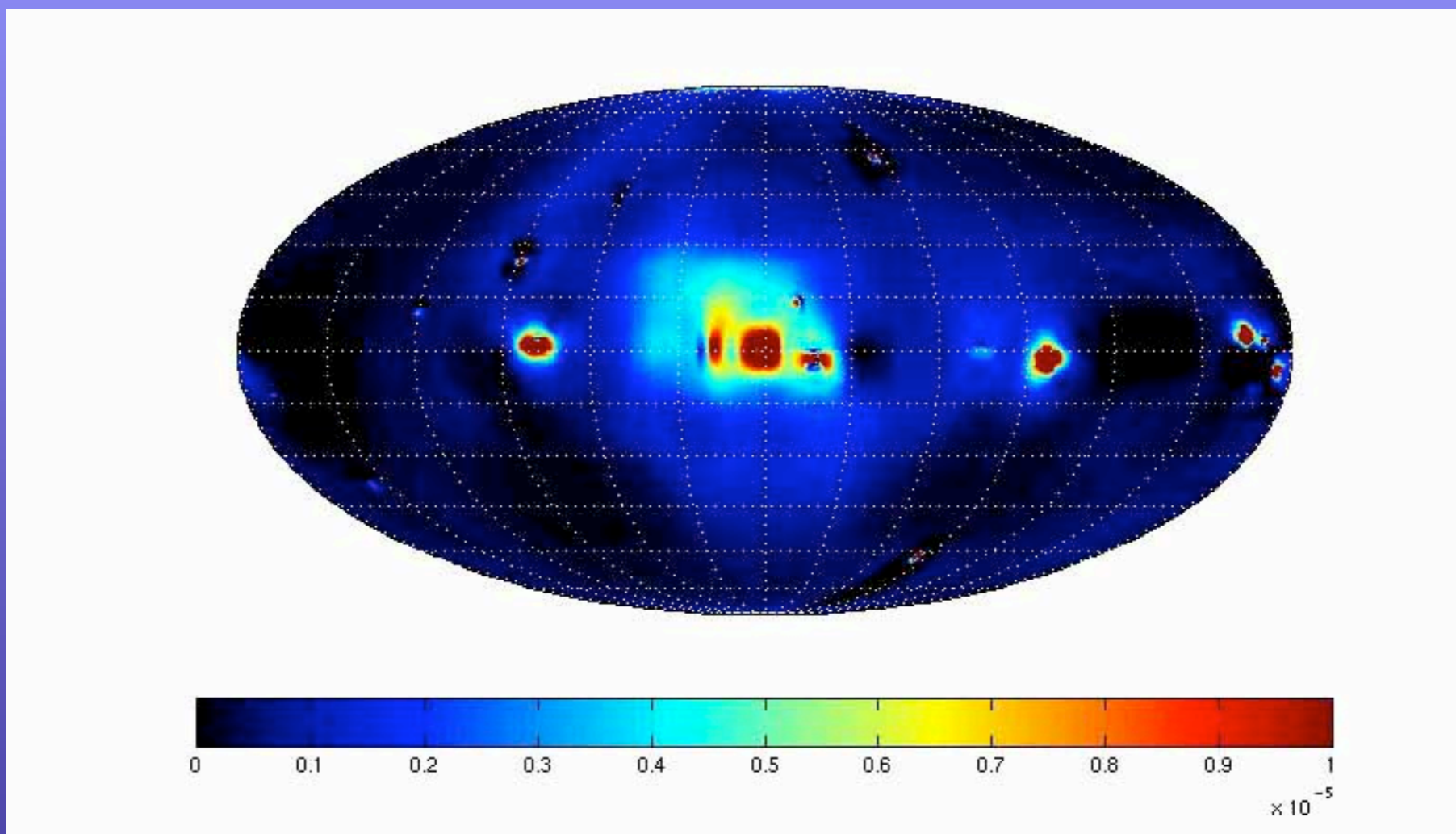
### Some Radioactive Decays

-   $\alpha$  decay (Helium-4 Nucleus)
-   $\beta^-$  decay (electron)
-   $\gamma$  decay (gamma-ray photon)
-  proton decay (spherical nucleus)
-  proton decay (deformed nucleus)





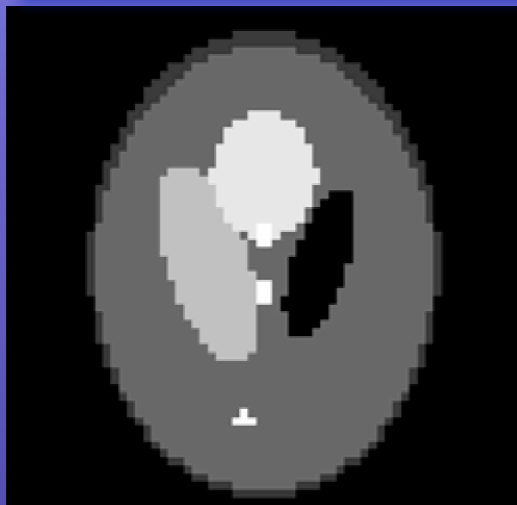
`The immediate question arises as to the statistical significance of this feature... quantification of object-wise significance (e.g., "this blob is significant at the n-sigma level") are difficult.' (Dixon et al. 1998 New Astronomy 3, 539)



`The immediate question arises as to the statistical significance of this feature... quantification of object-wise significance (e.g., "this blob is significant at the n-sigma level") are difficult.' (Dixon et al. 1998 New Astronomy 3, 539)

# Tomographic Reconstruction: Comparing Examples (from Willett et al.)

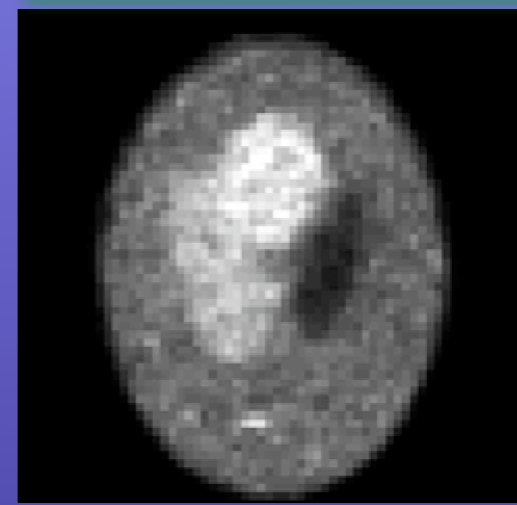
True image



Filtered back projection



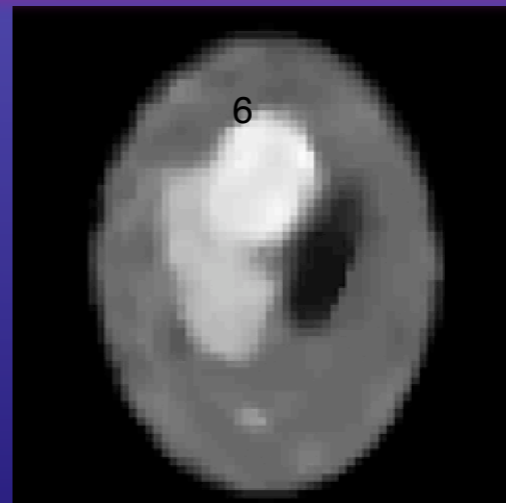
MLE reconstruction



Fessler's PWLS



Wedgelet reconstruction



What's the significance of / uncertainty on features?

# Talk Outline (Parallel pieces):

0. What/Why: Demos, Definitions

1. What/Why: Problem Definition:

1.1 Goodness-of-fit and feature-detection

1.2 Mismatch significance, shape error bars

1.3 All uncertainties: instrument, physics

2. How/Why: History/Methods

2.1 Frequentist Multiscale, Bayesian Structure

2.2 DA/MCMC

2.3 Comparisons of Null (simulations) vs Data

3. Current Examples

Varying signal to noise: "E" and Gamma-ray sky

4. Current Challenges

# How/Why: History/Methods

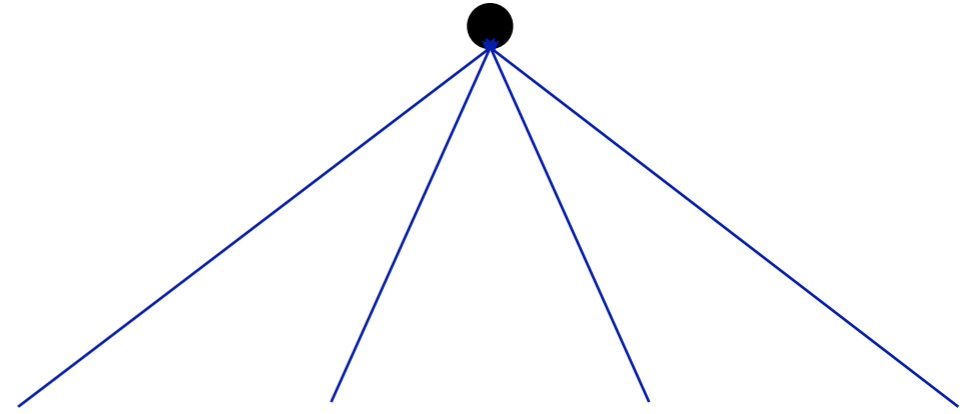
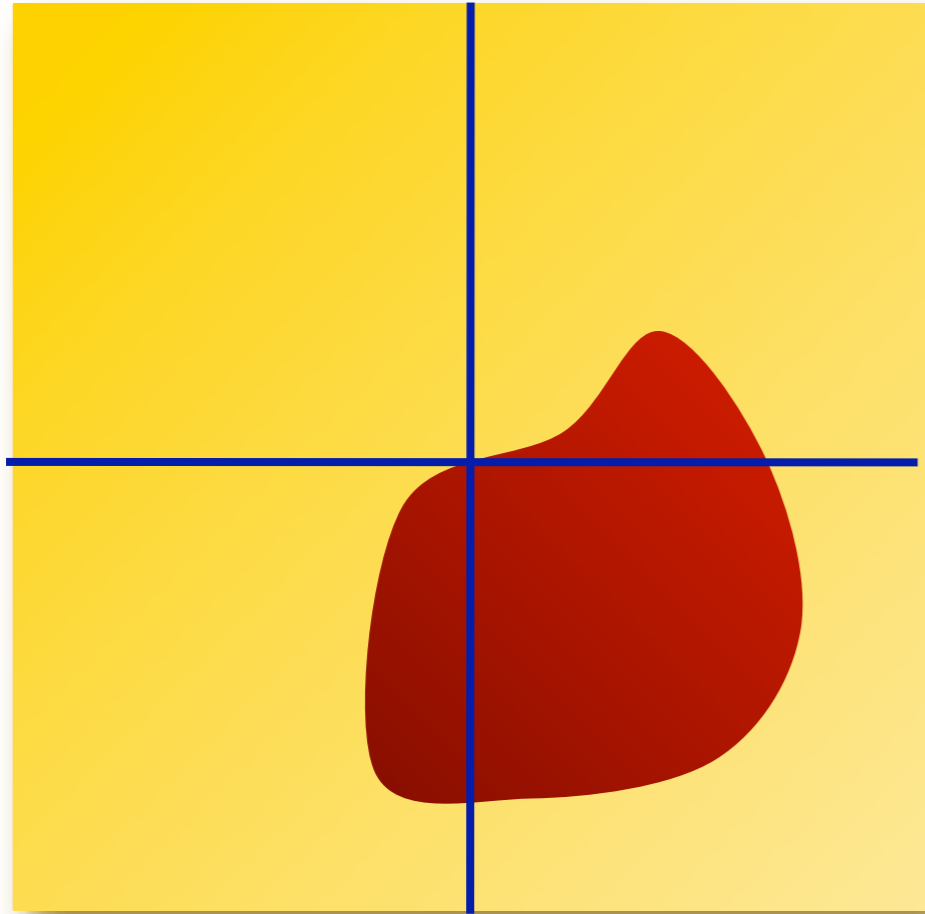
- \* Putting Flexible/Multiscale 'NP' models
- \* Together with parametrized physics-based models
- \* Full Bayesian Posterior framework
  
- \* 'Likelihoodist' (Tanner); Priors  $\sim$  Complexity Penalty
- \* Bayes allows Modularity: Data Augmentation,
- \* Bayes allows complex, high-dimensions: MCMC



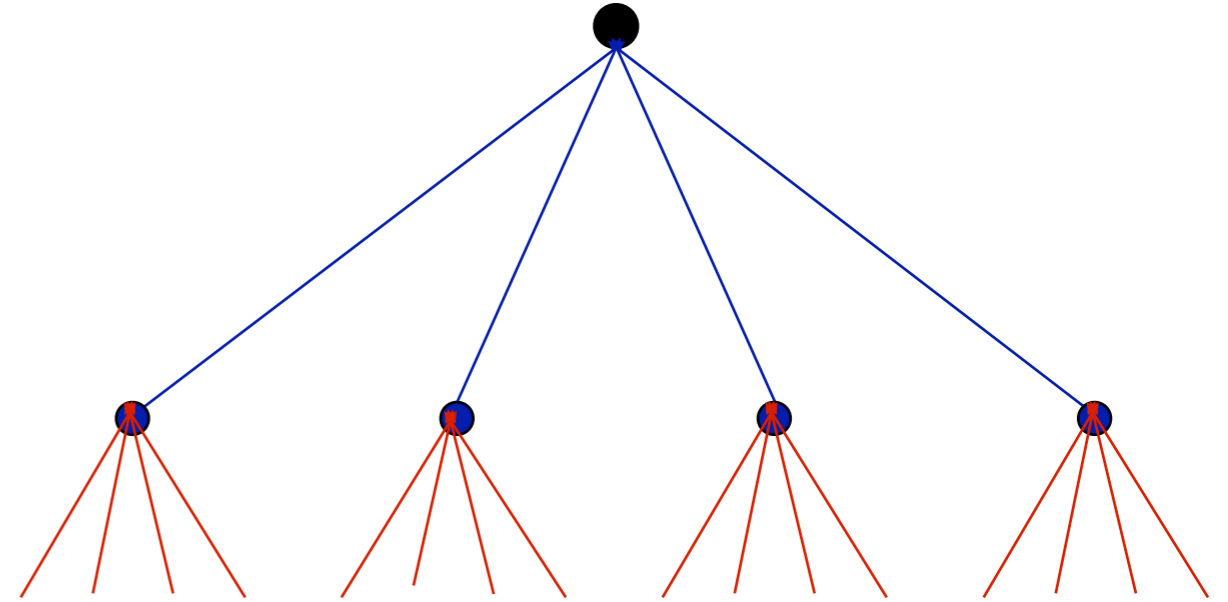
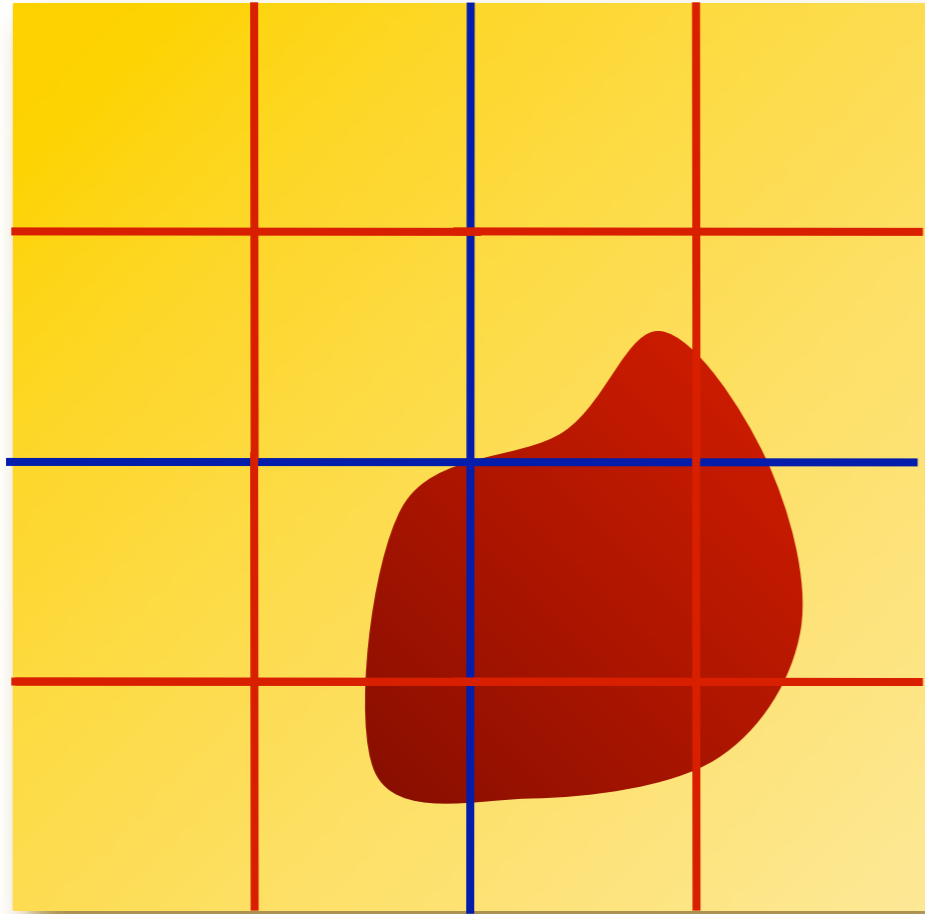
# Multiplicative Multiscale Innovation Models



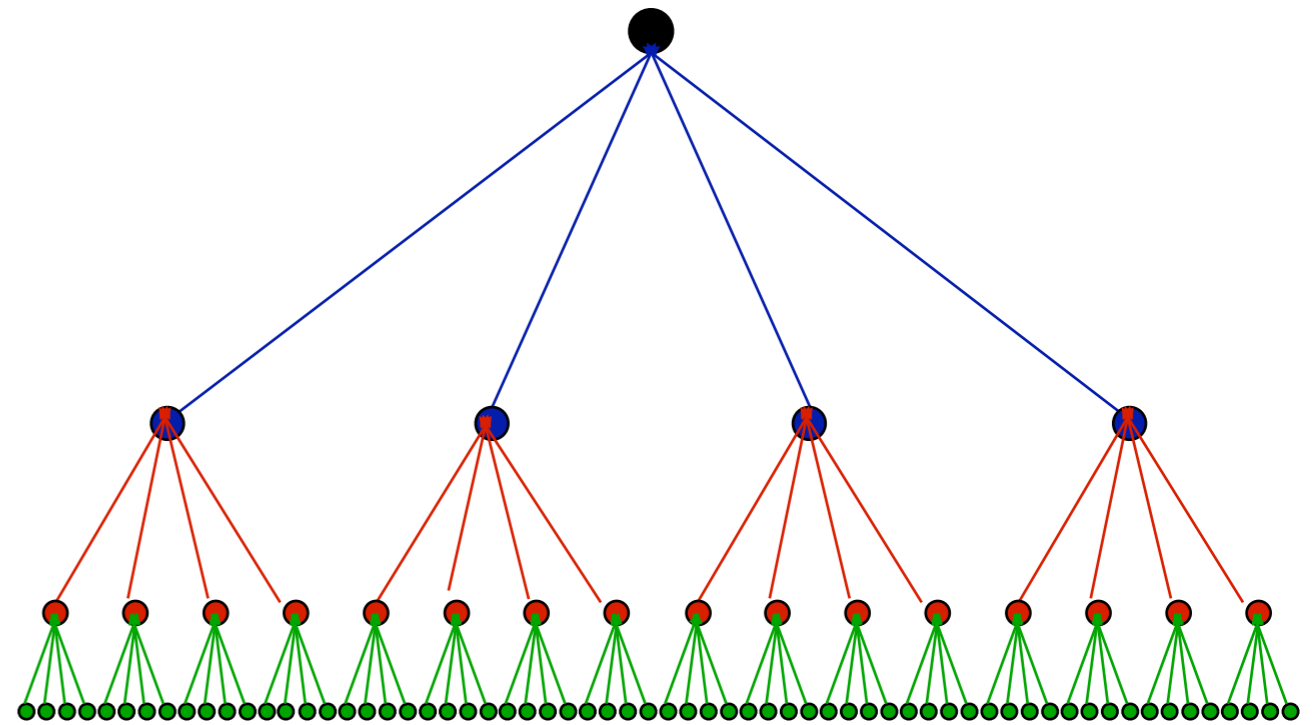
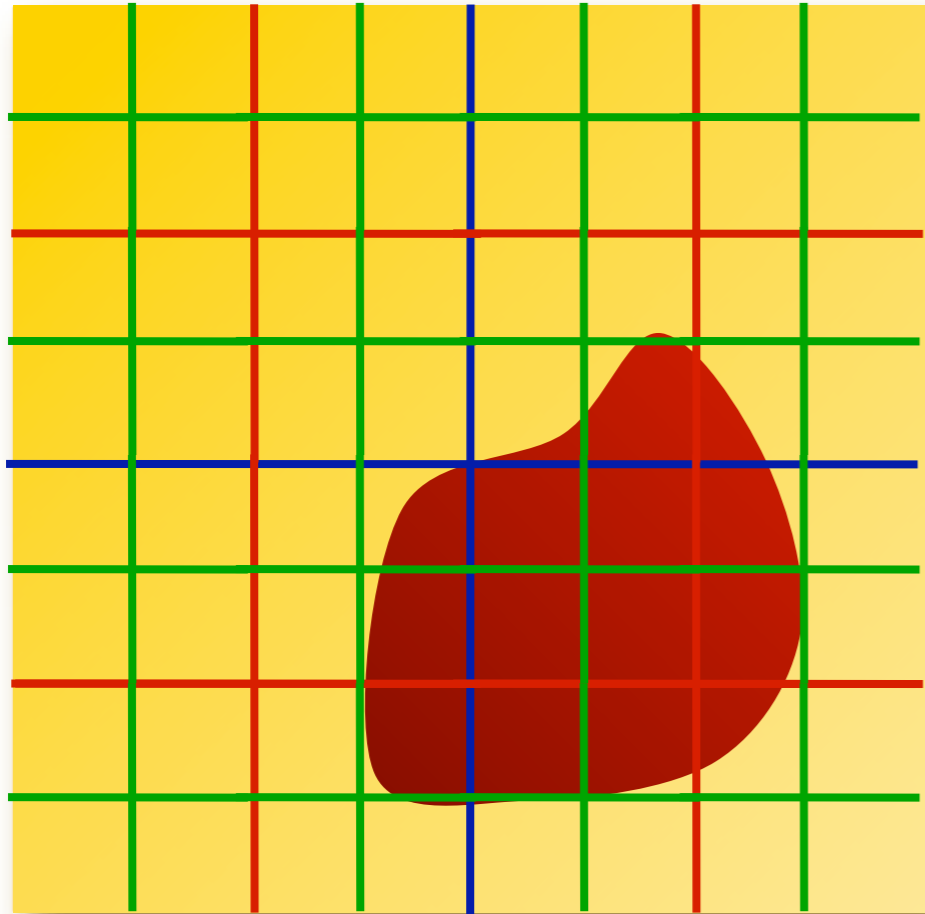
# Multiplicative Multiscale Innovation Models



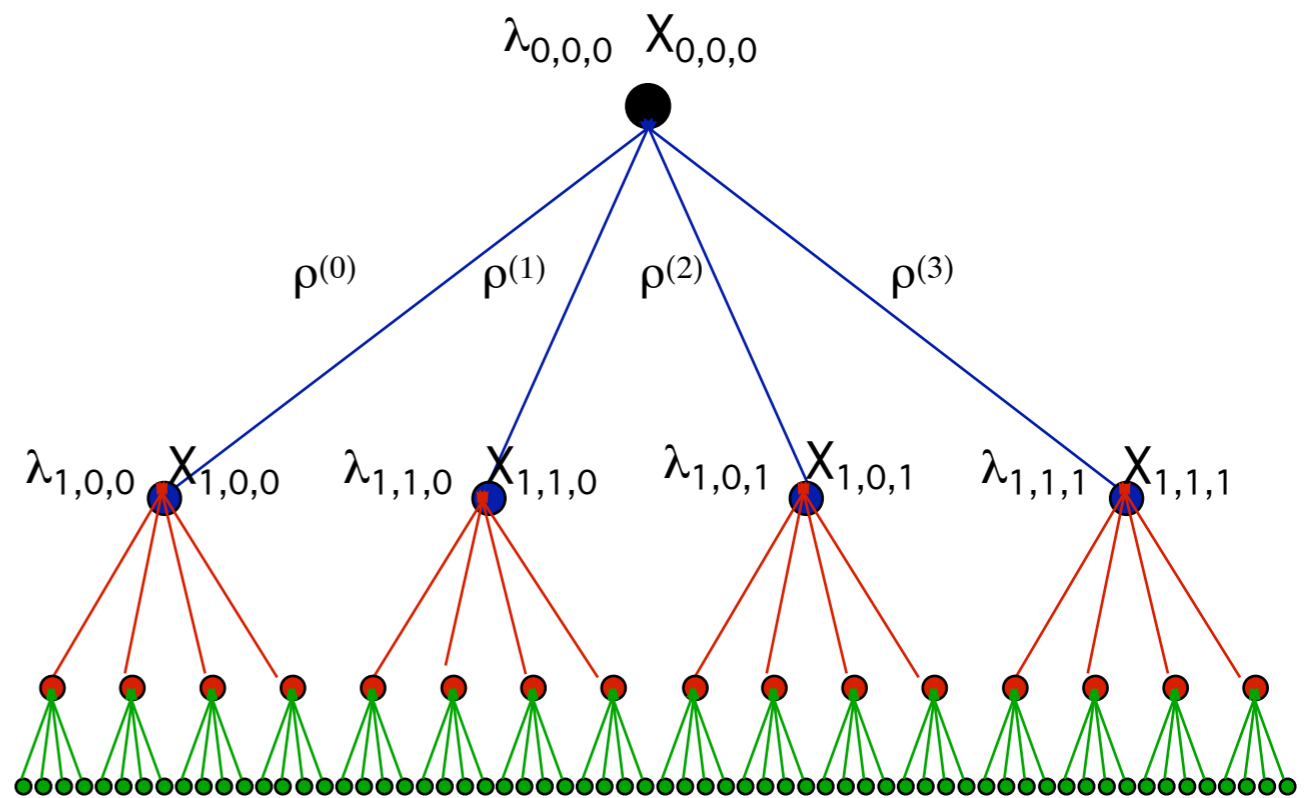
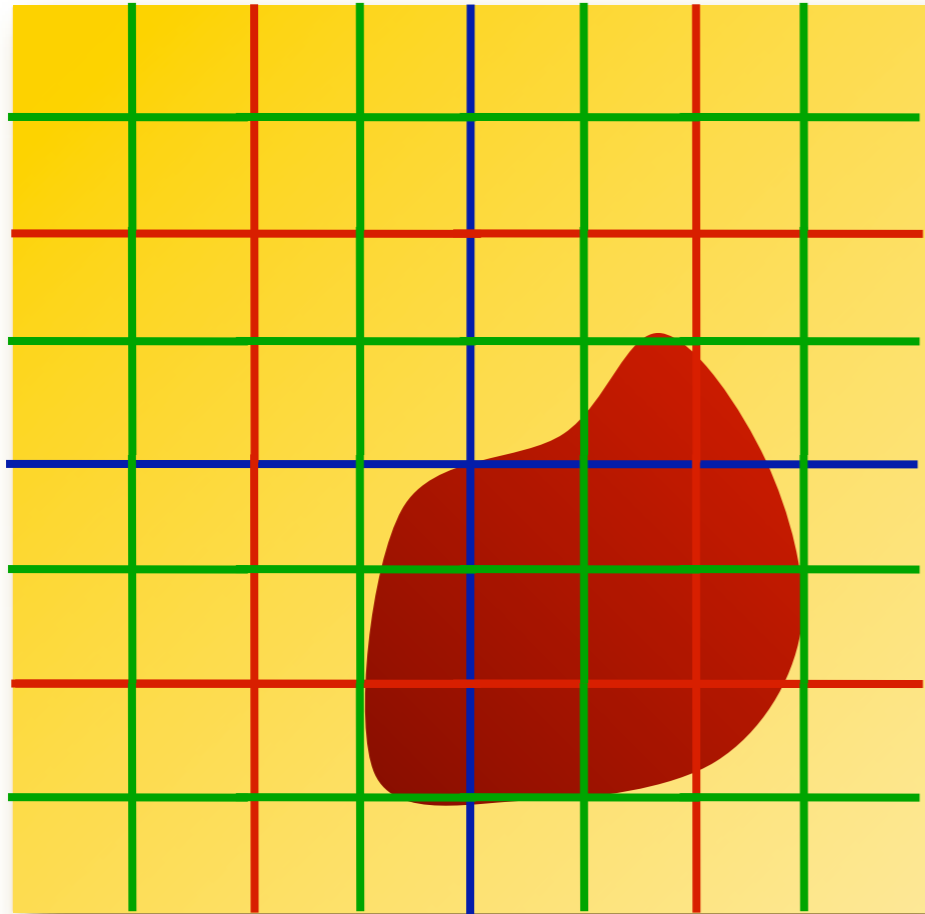
# Multiplicative Multiscale Innovation Models



# Multiplicative Multiscale Innovation Models



# Multiplicative Multiscale Innovation Models



- Recursively subdivide image into squares
- Let  $\{\rho\}$  denote the ratio between child and parent intensities
- Knowing  $\{\rho\} \Leftrightarrow$  Knowing  $\{\lambda\}$
- Estimate  $\{\rho\}$  from empirical estimates based on counts in each partition square

## Usual Equations for 'True' Intensity, Instrument, Data:

$S(l,b,e,t,\theta)$  = Expected 'True' Source Intensity

$E(l,b,e,t,\varphi)$  = 'True' Effective Area

$PSF(x,y | l,b,e,t,\xi)$  = 'True' instrument smearing

$\Lambda(x,y,e,t,\theta,\varphi,\xi)$  = 'True' Expected counts in detector

$D(x,y,e,t,\theta,\varphi,\xi)$  = measured counts in detector

$$\Lambda(x,y,e,t,\theta,\varphi,\xi) = PSF(x,y|l,b,e,t,\xi) @ E(l,b,e,t,\varphi) * S(l,b,e,t,\theta)$$

$$D(x,y,e,t,\theta,\varphi,\xi) \sim \text{Poisson}(\Lambda(x,y,e,t,\theta,\varphi,\xi))$$

## Usual Equations for 'Model' Intensity, Instrument, Data:

$s(l,b,e,t,\theta)$  = Expected 'Model' Source Intensity

$\epsilon(l,b,e,t,\varphi)$  = 'Model' Effective Area

$\text{psf}(x,y \mid l,b,e,t,\xi)$  = 'Model' instrument smearing

$\lambda(x,y,e,t,\theta,\varphi,\xi)$  = 'Model' Expected counts in detector

$D(x,y,e,t,\theta,\varphi,\xi)$  = measured counts in detector

$$\lambda(x,y,e,t,\theta,\varphi,\xi) = \text{psf}(x,y \mid l,b,e,t,\xi) @ \epsilon(l,b,e,t) * s(l,b,e,t,\theta)$$

$$D(x,y,e,t,\theta,\varphi,\xi) \sim \text{Poisson}(\lambda(x,y,e,t,\theta,\varphi,\xi))$$

## Our Equations for 'Model' Intensity, Instrument, Data:

$s(l,b,e,t,\theta)$  = Expected 'Physics Model' Source Intensity

→  $m(l,b,e,t,\alpha,\kappa)$  = Expected Multiscale Source Counts

$\alpha$  = Smoothing Parameters for each scale

$\kappa$  = 'Range' parameter for Hyper-priors on  $\alpha$

→  $\beta$  = 'Scale Factor' for Physics Model

$\epsilon(l,b,e,t,\varphi)$  = 'Model' Effective Area

$\text{psf}(x,y \mid l,b,e,t,\xi)$  = 'Model' instrument smearing

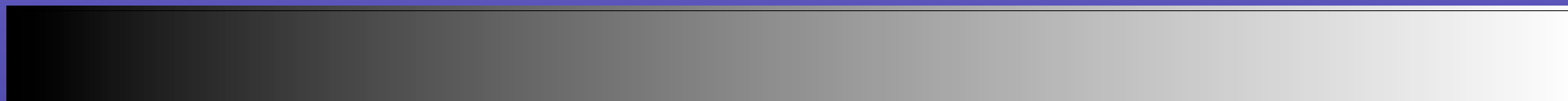
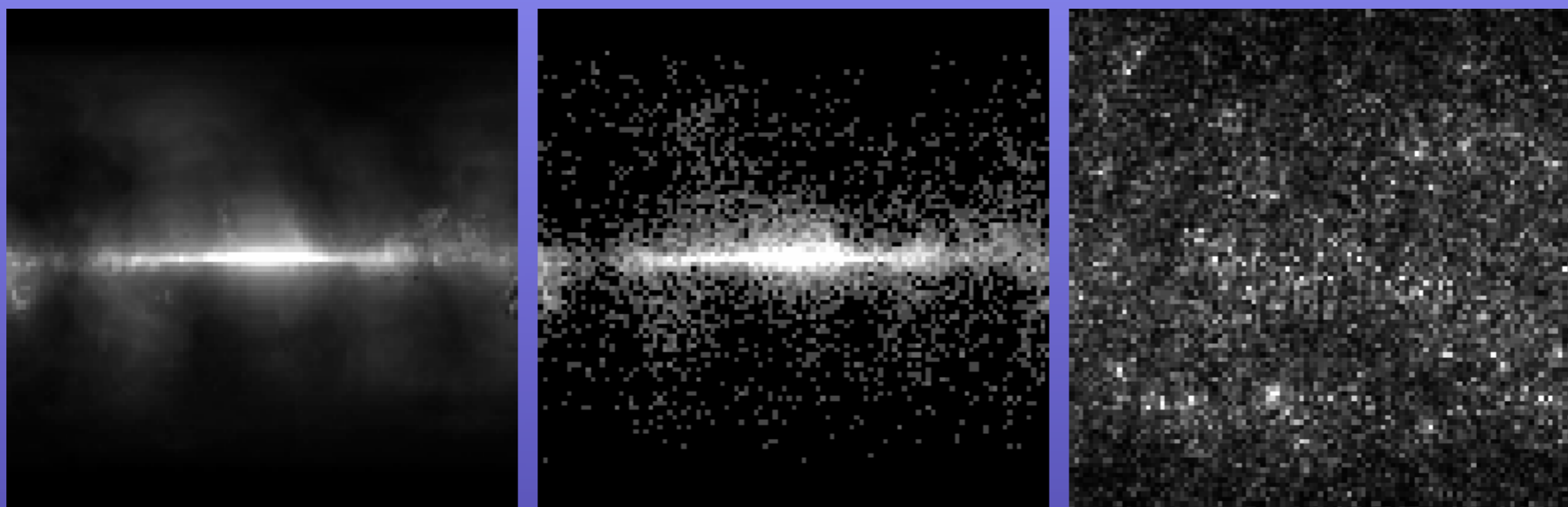
$\lambda(x,y,e,t,\theta,\varphi,\xi)$  = 'Model' Expected counts in detector

$D(x,y,e,t,\theta,\varphi,\xi)$  = measured counts in detector

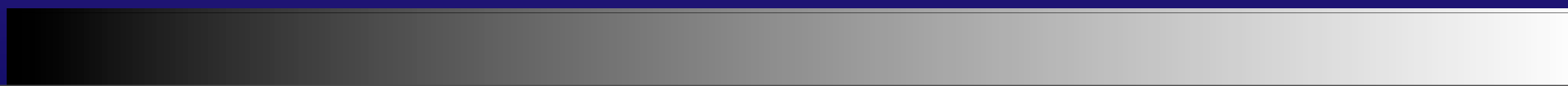
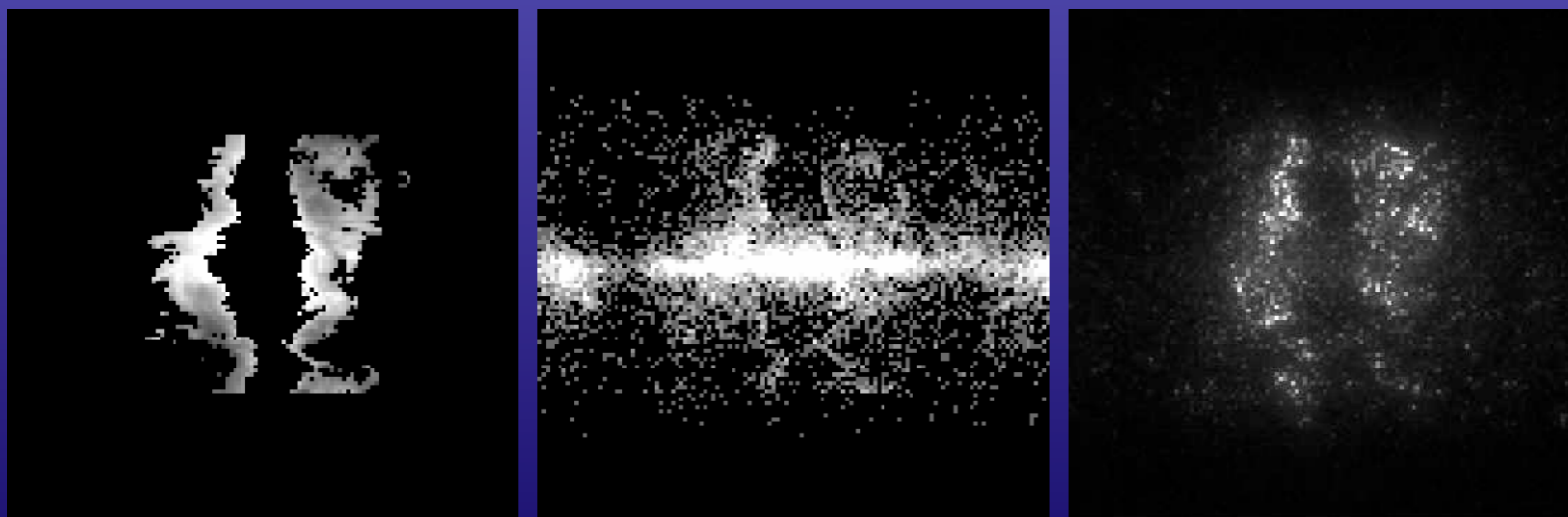
$$\lambda(x,y,e,t,\theta,\varphi,\xi) = \text{psf}(x,y \mid l,b,e,t,\xi) @$$
$$(\beta^* \epsilon(l,b,e,t) * s(l,b,e,t,\theta) + m(l,b,e,t,\alpha,\kappa))$$



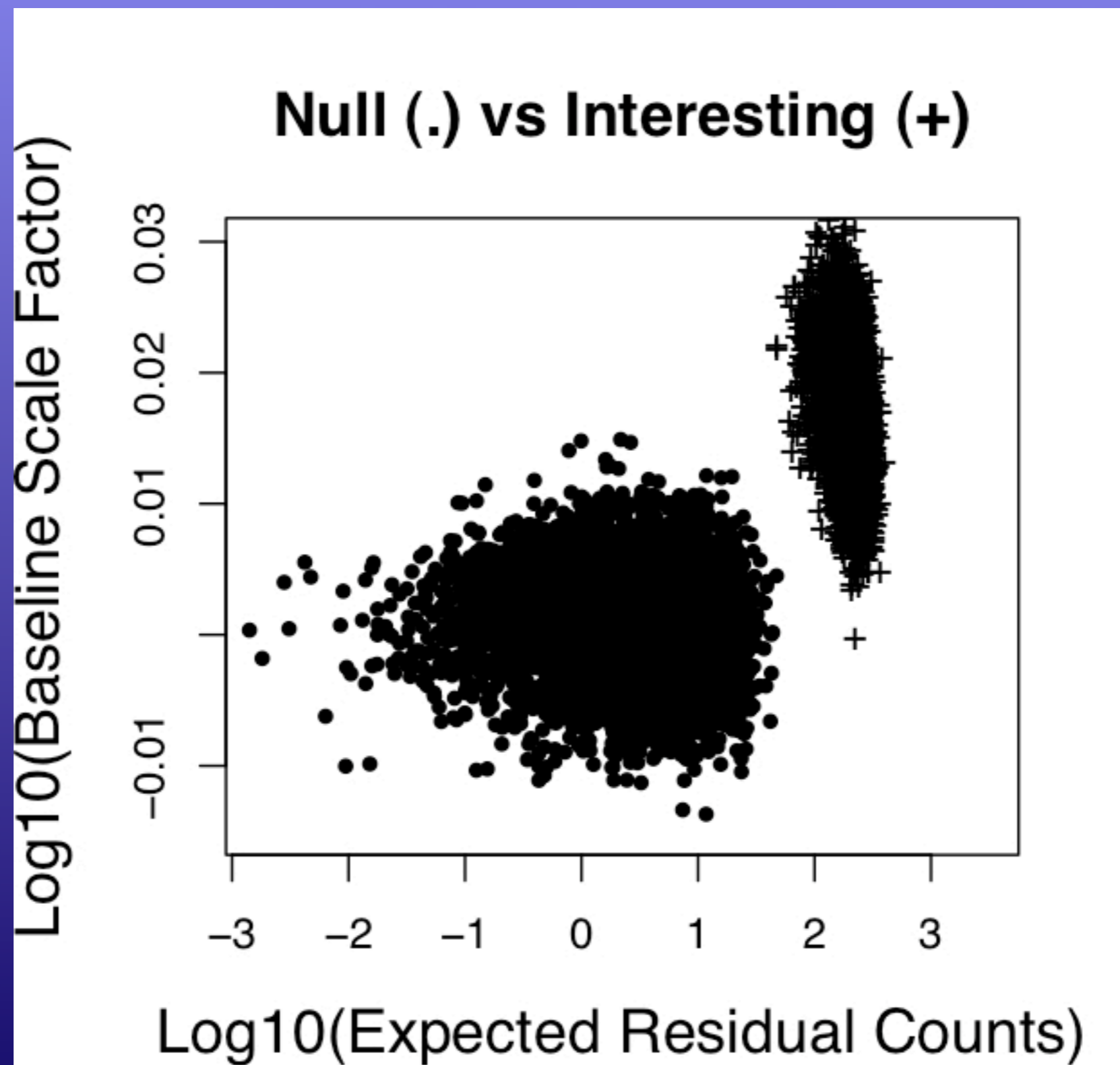
### 3. Moderate Signal-To-Noise Examples: Gamma-Ray Sky:



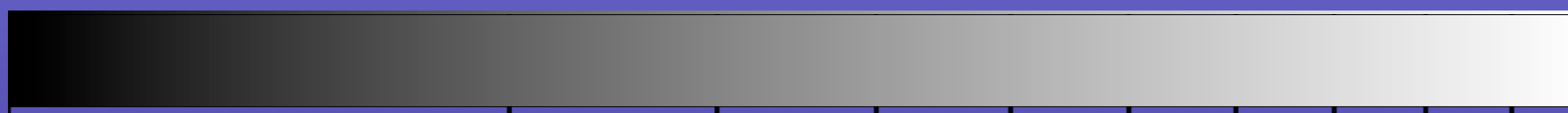
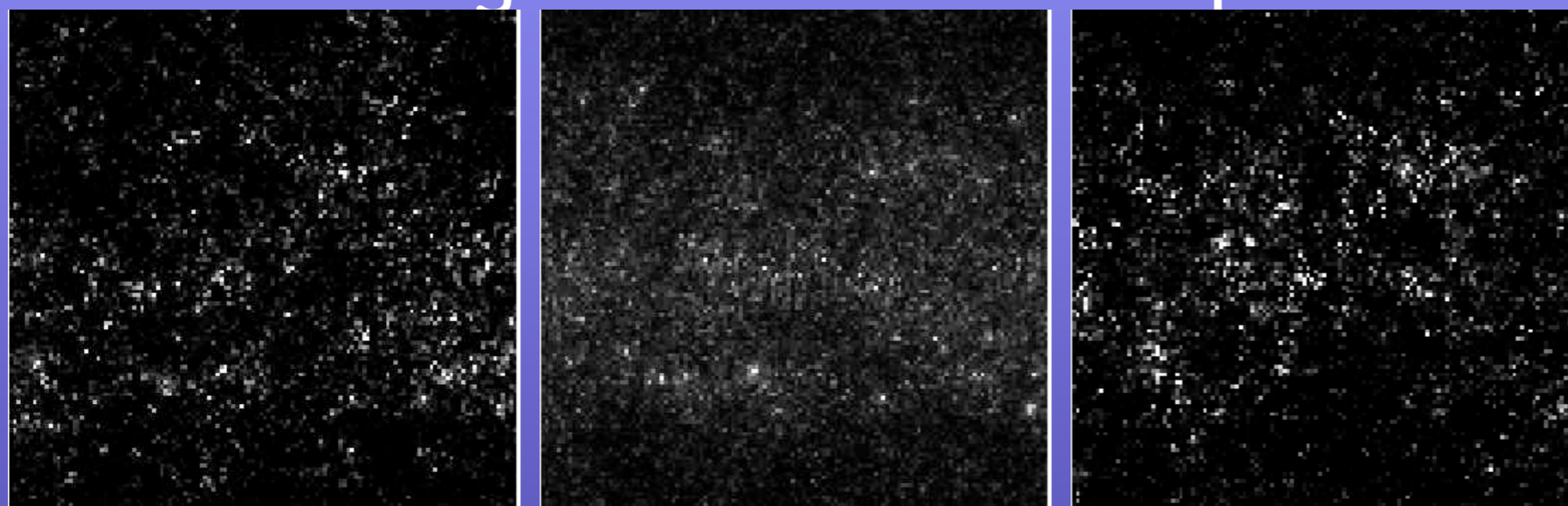
) 5 10 15 20



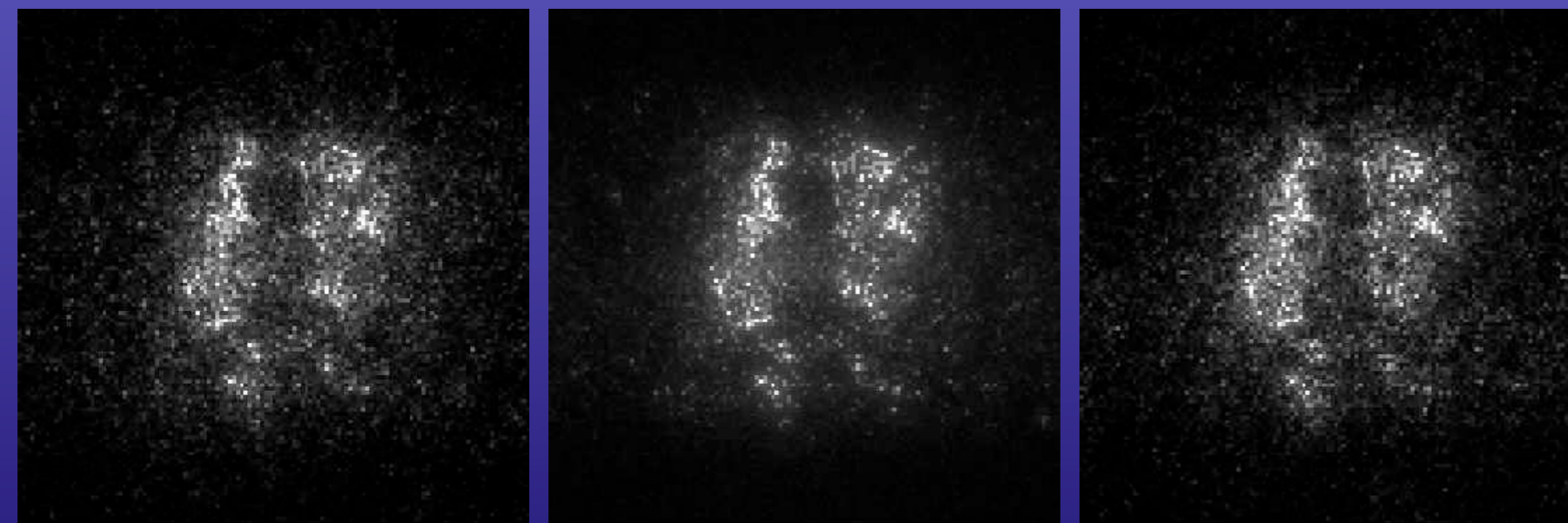
### 3. Moderate Signal-To-Noise Examples:Gamma-Ray Sky:



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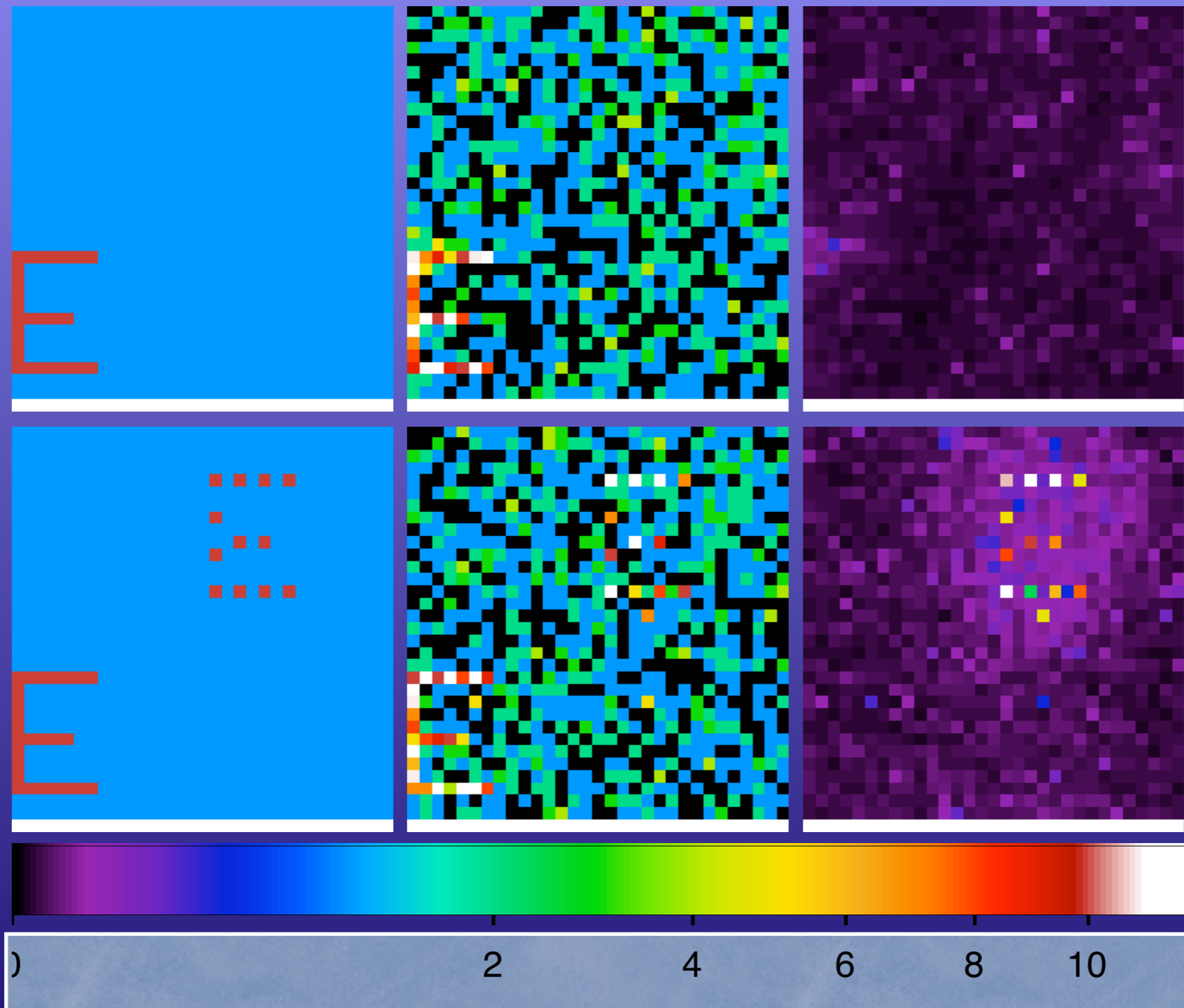


0.004 0.008 0.012 0.016

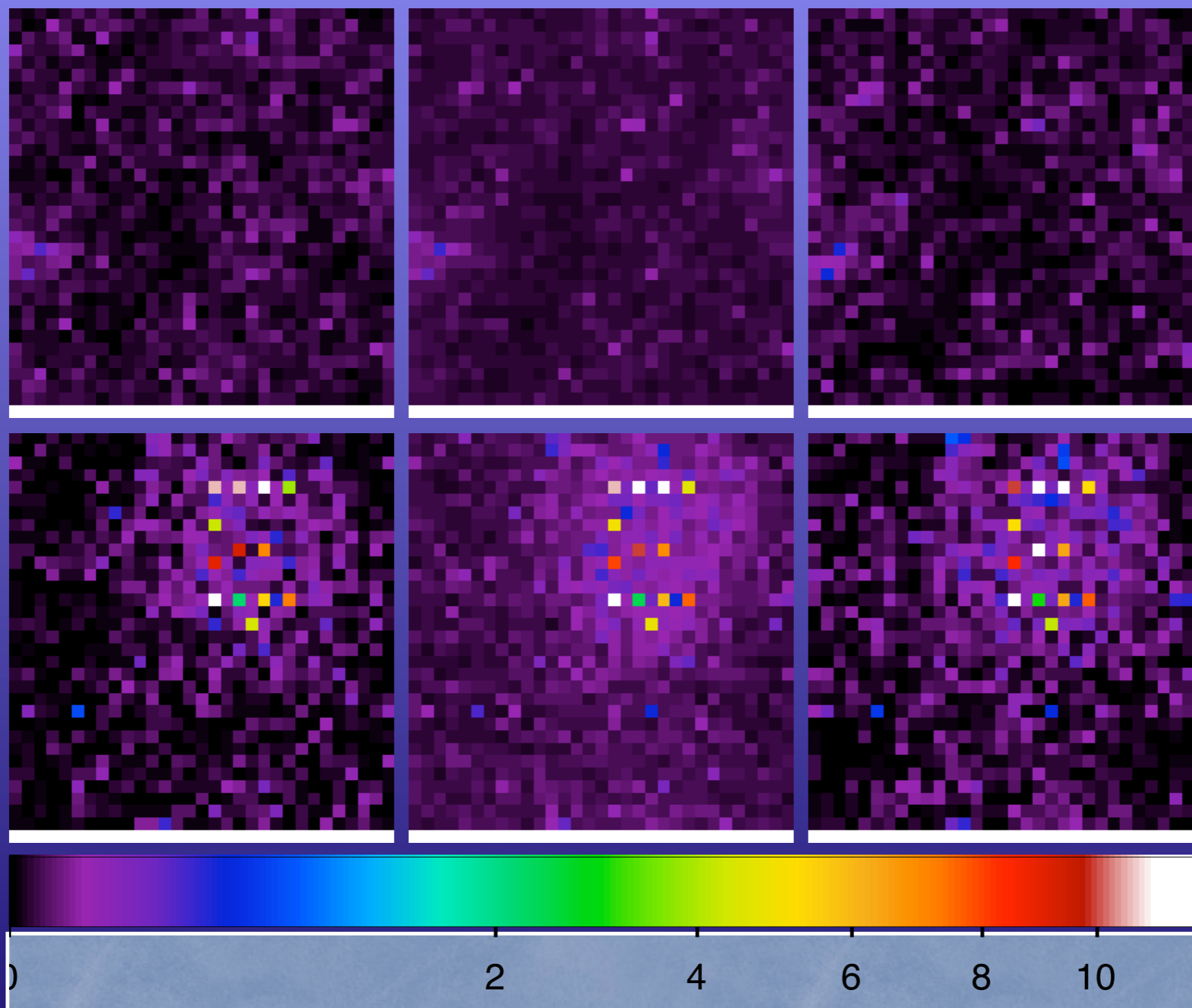


0.05 0.1 0.15 0.2 0.25 0.3 0.35 0.40 0.45

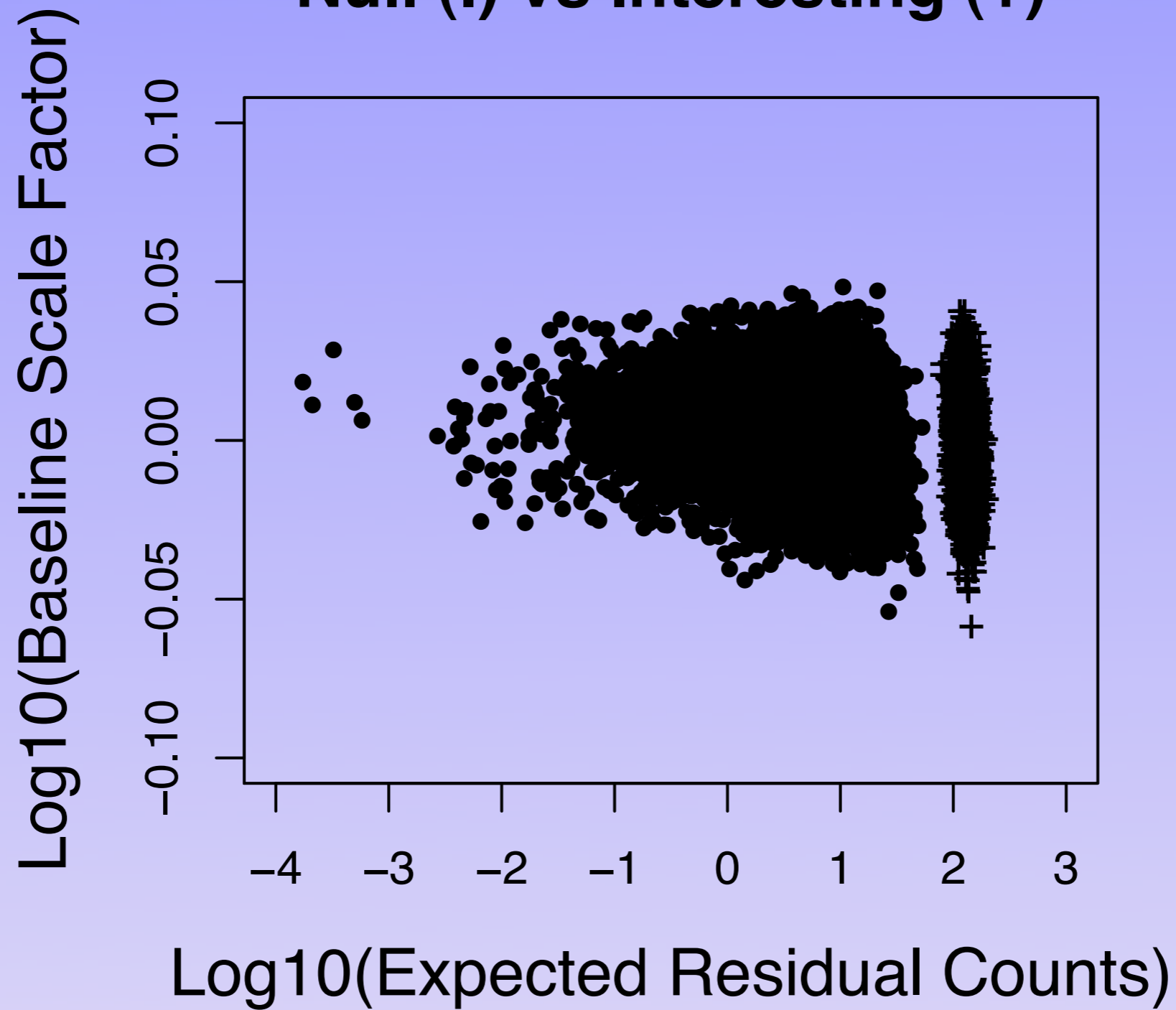
# 4. Moderate Signal-To-Noise Examples: 2 "E":



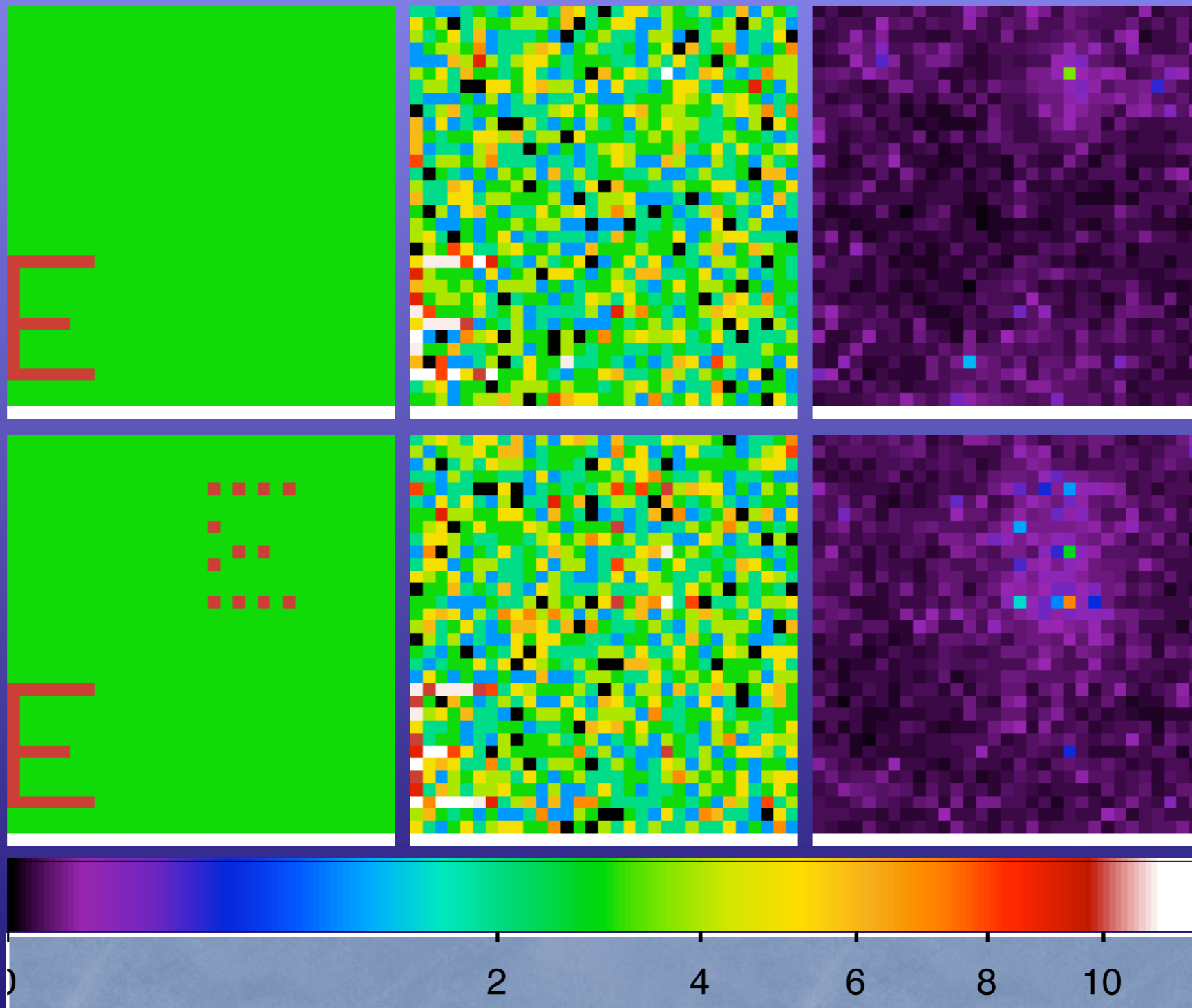
# 4. Moderate Signal-To-Noise Examples: 2 "E":



4. Moderate Signal-To-Noise Examples: 2 "E":  
**Null (.) vs Interesting (+)**

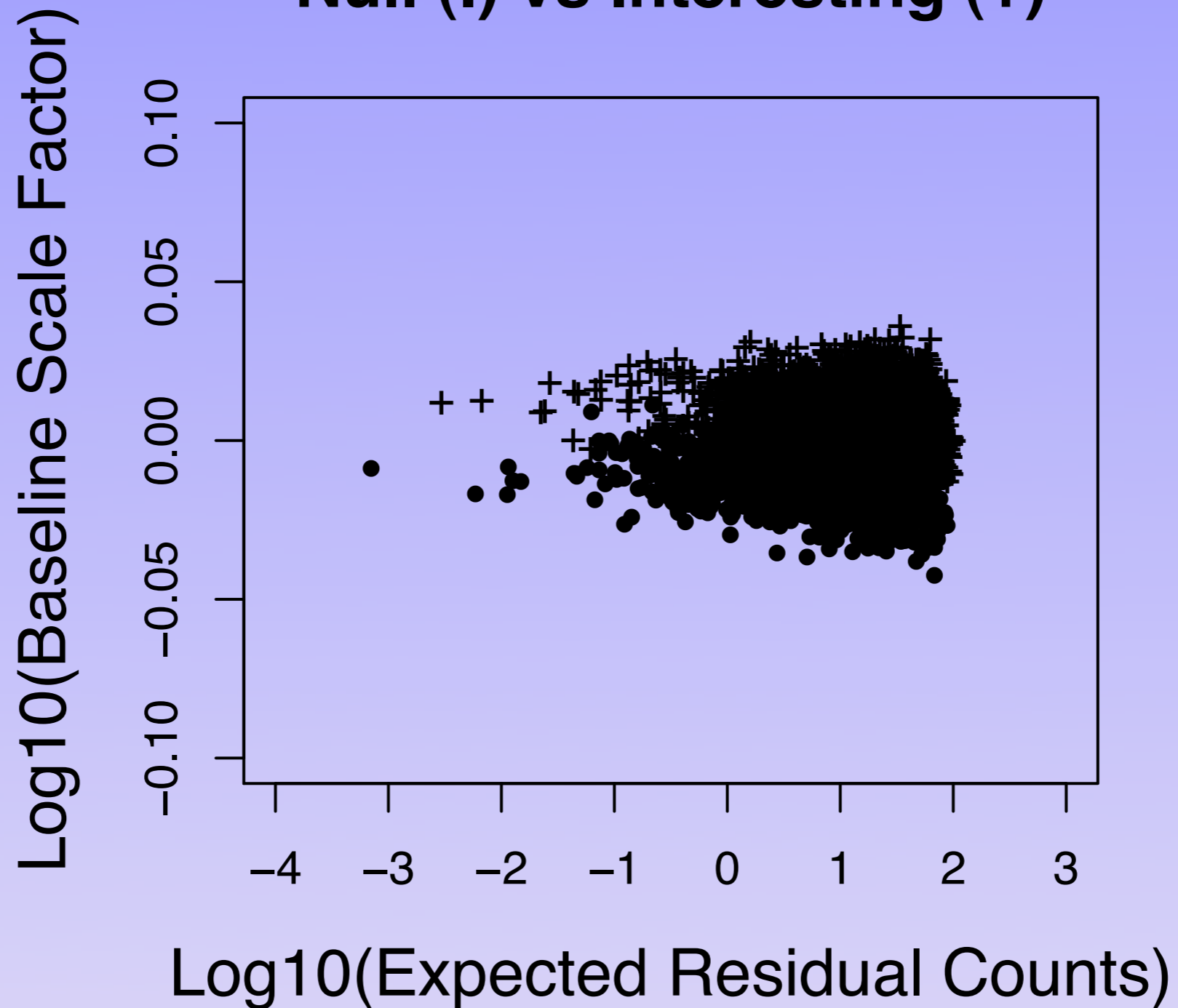


### 3. Low Signal-To-Noise Examples: 2 "E":



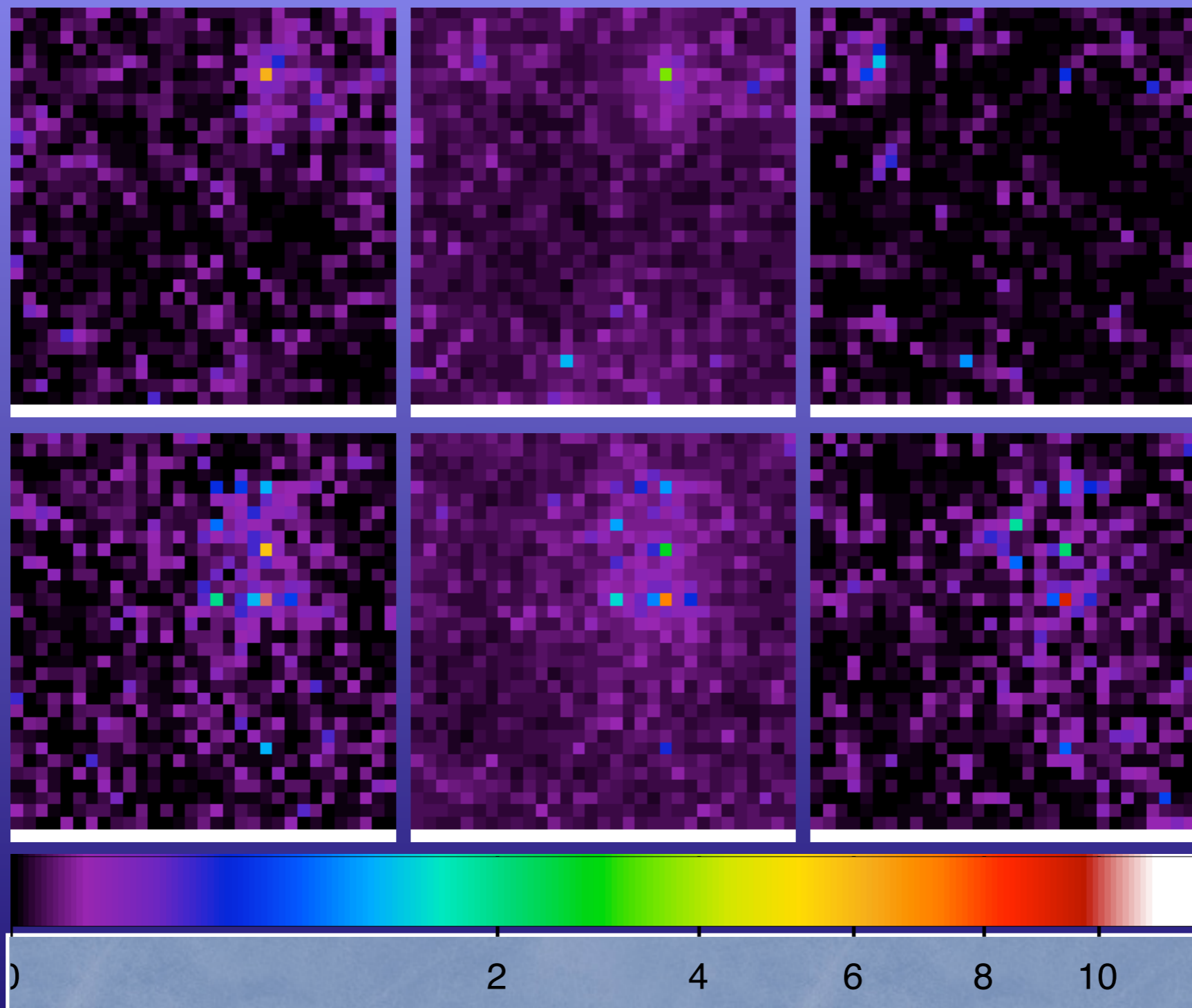
## 5. Low Signal-To-Noise Examples: 2 "E":

**Null (.) vs Interesting (+)**



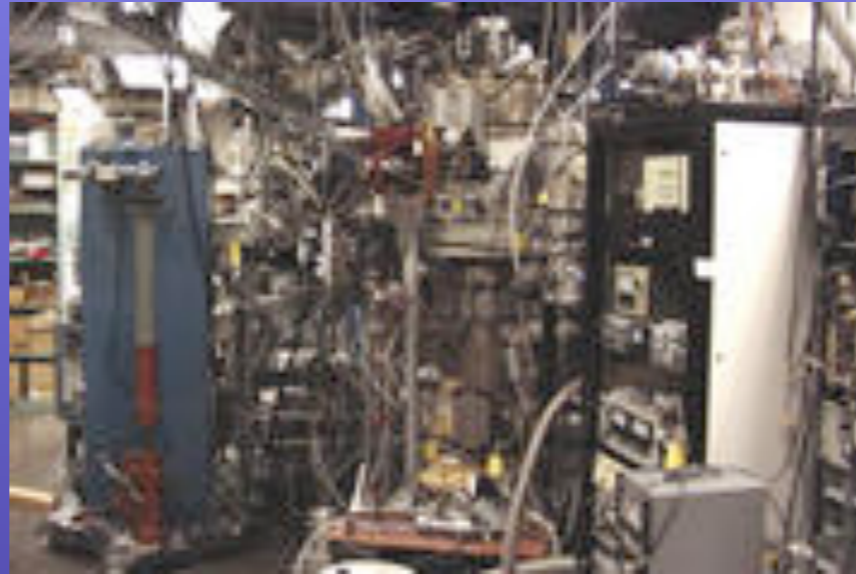


## 5. Low Signal-To-Noise Examples: 2 "E":

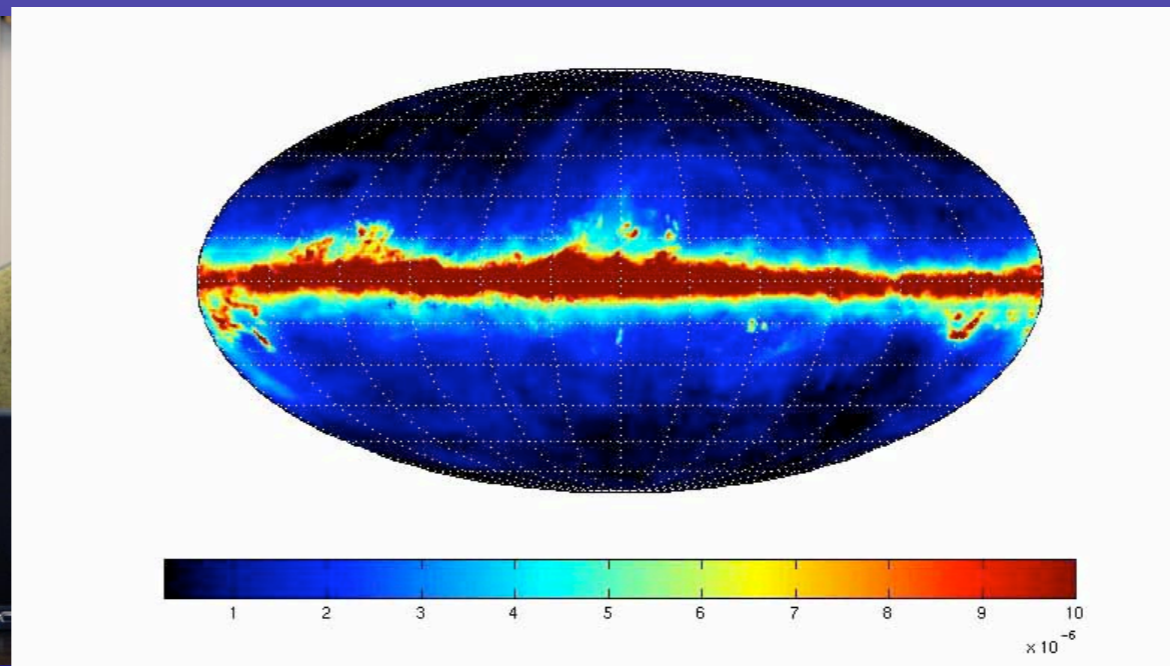


# DOUBT: Skeptical Astronomers: Basic Physics??

V. Kashyap, N. Brickhouse : Atomic physics uncertainty



I. A. Grenier, J. M Casandjian : "GALPROP" uncertainty



DOUBT: Skeptical Astronomers.....  
J. Drake, et al. : ARF/RMF uncertainty



## DOUBT: Skeptical Astronomers.....

M. Karovska on PSF Variations/Uncertainty:

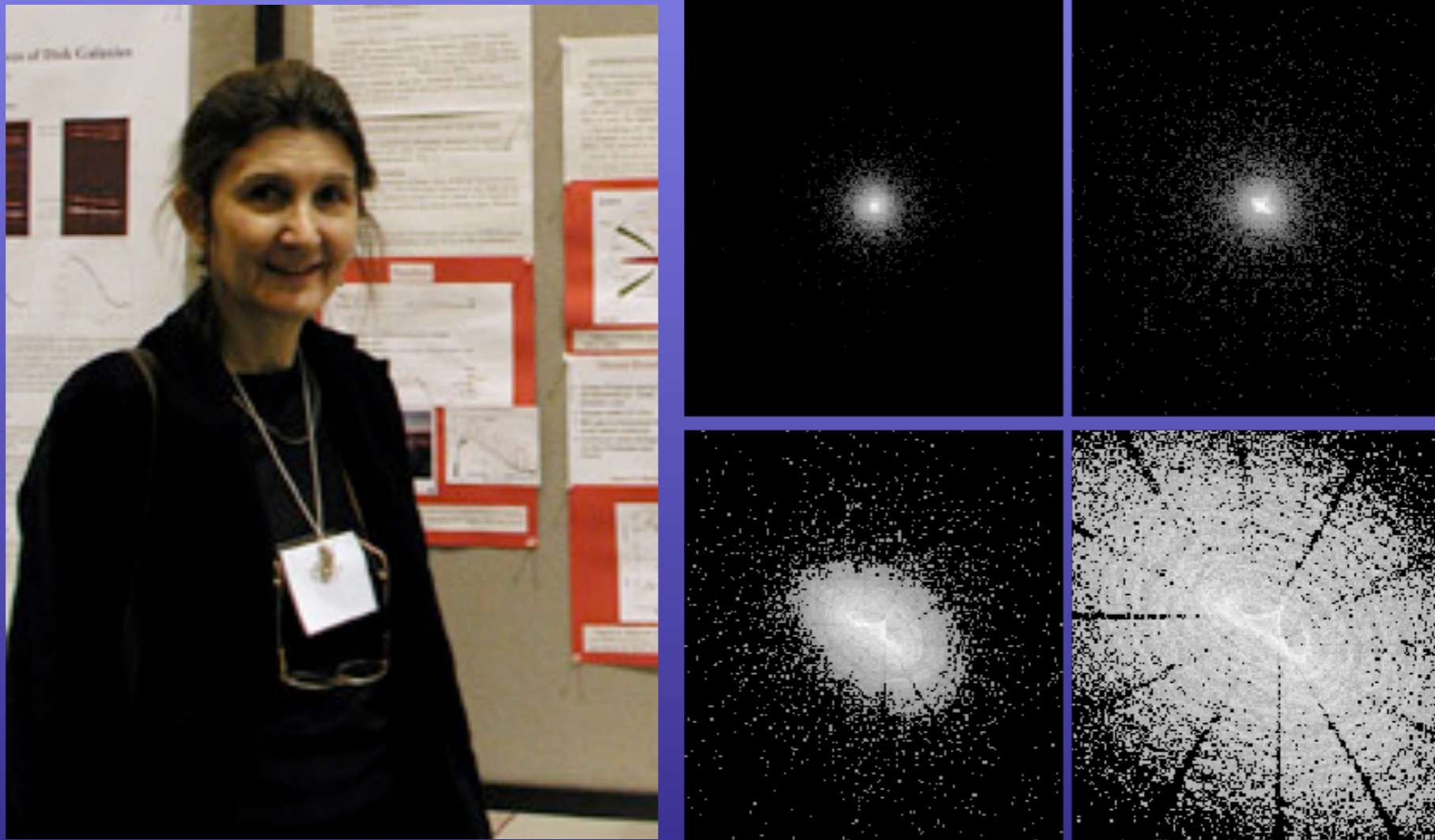
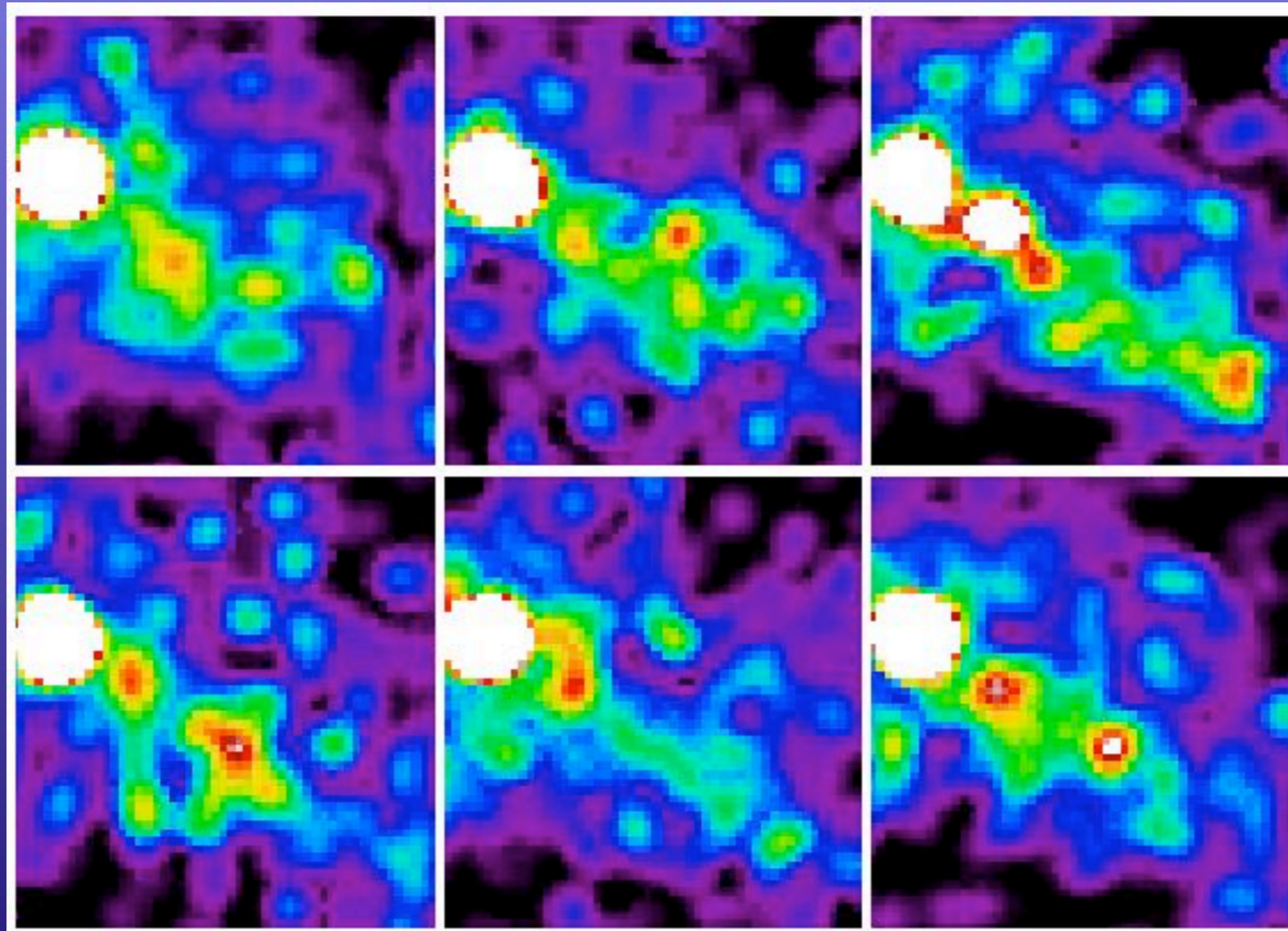
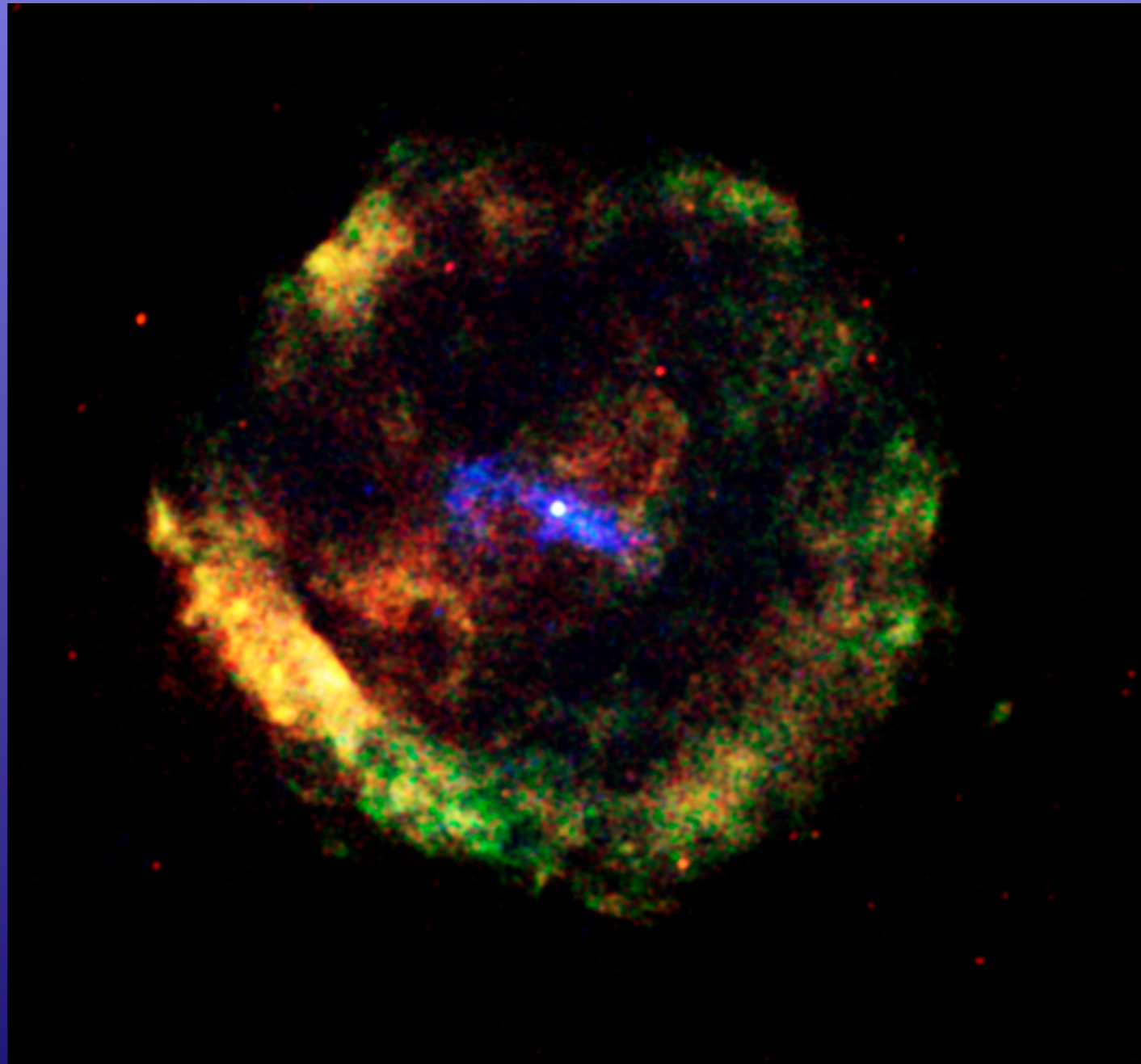


Figure: Model PSFs for the HRC-I instrument at 1.4967keV as a function of off-axis angles (log display); clockwise from the top, off-axis angles 0' (on axis), 1.5', 6', and 12'. The size of the FOV is about 0.5'.

# NEW CHALLENGES: Examples (Mallory Roberts -Black Hole/Jet changes?)



NEW CHALLENGES: Examples  
SNR G11.2-0.3 changes with energy?  
Mallory Roberts



NEW CHALLENGES: Examples  
X-ray vs optical jet??  
Herman Marshall

